CS 277 - Experimental Haptics
Lecture 10

Deformable Models (II)

Outline

- Introduction
- Spring Models
- Computing Dynamics in the Haptics Loop
- Filling Sphere Approach for Elastic Models
- Computing Collision Detection in Real Time
- Demonstrations

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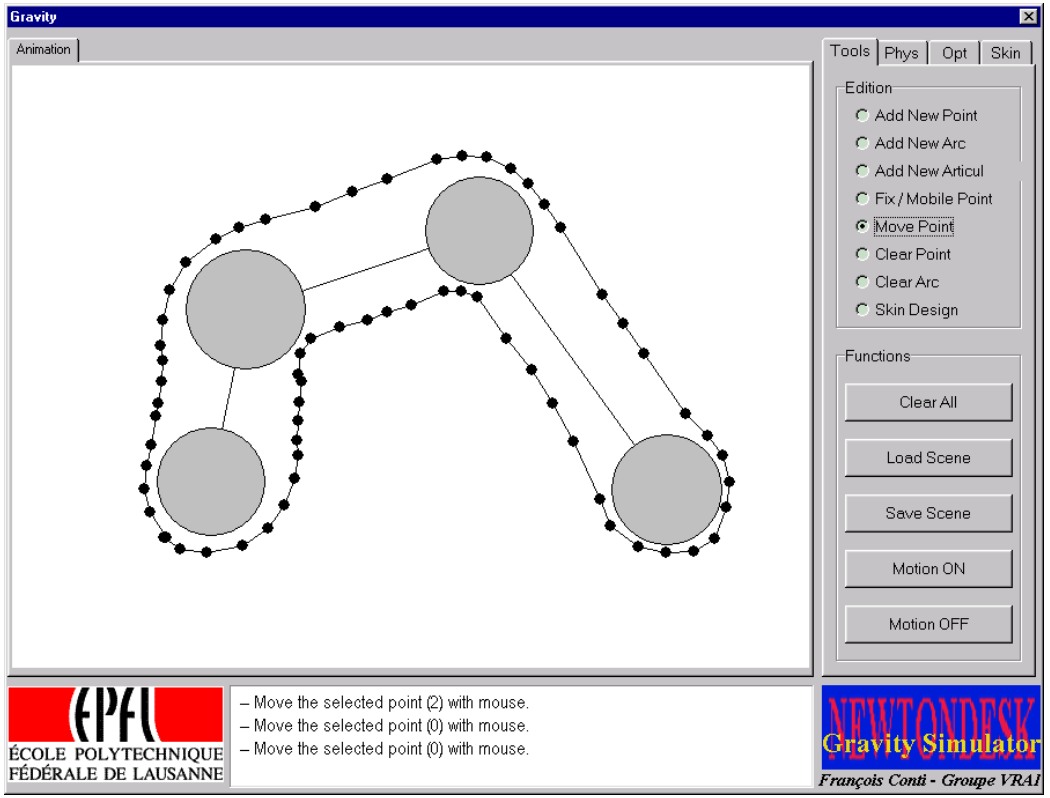
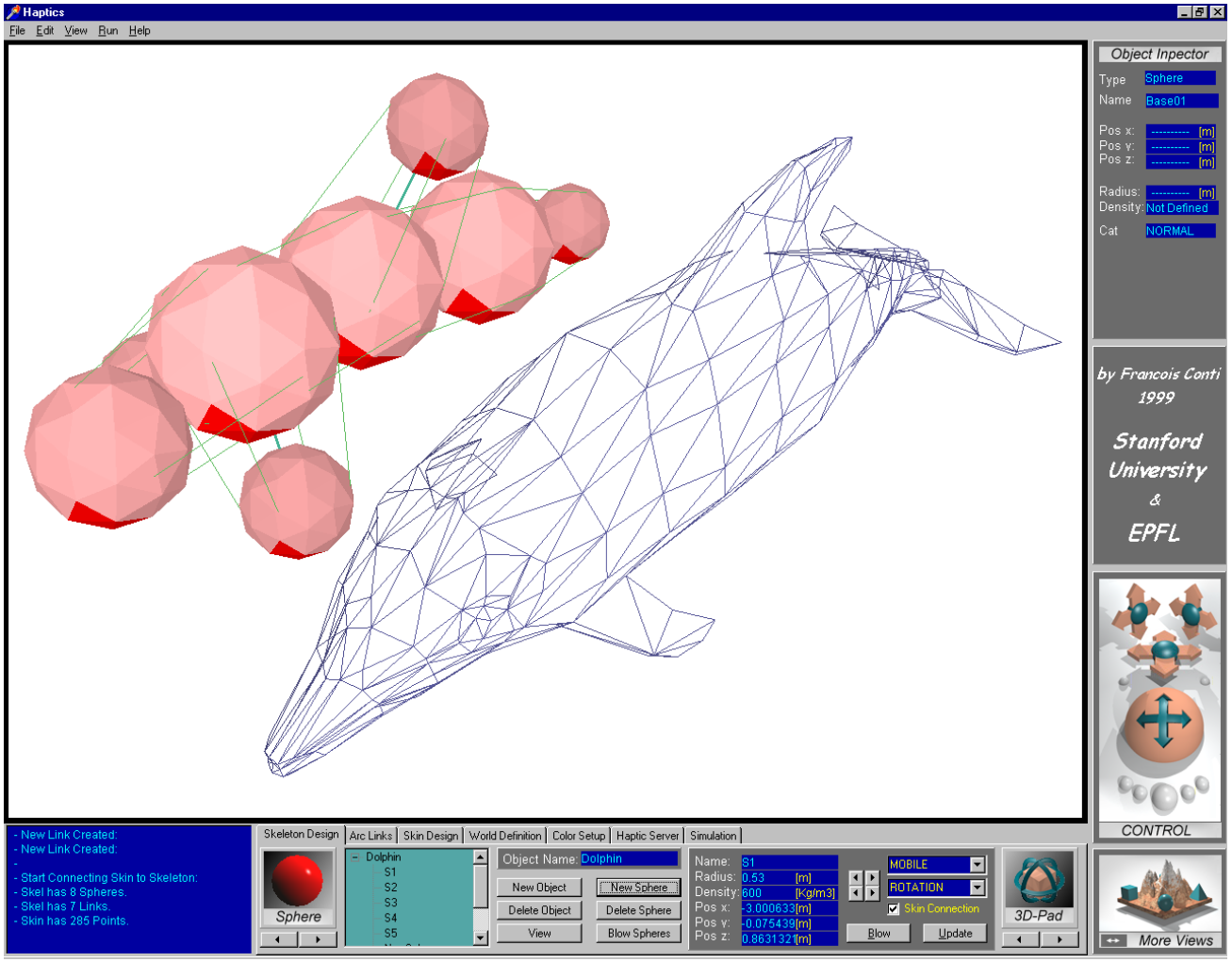
Filling Sphere Approach (2D)

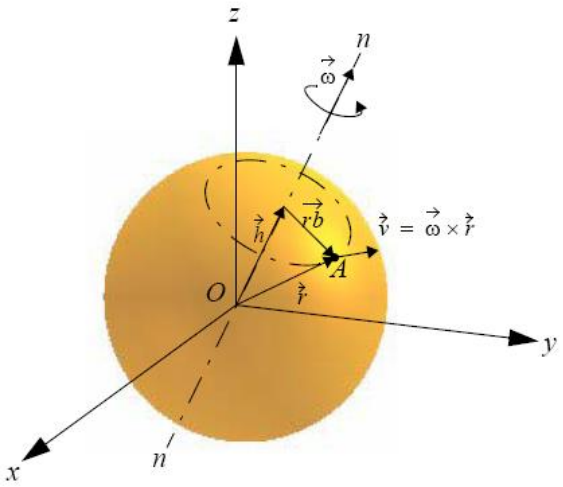


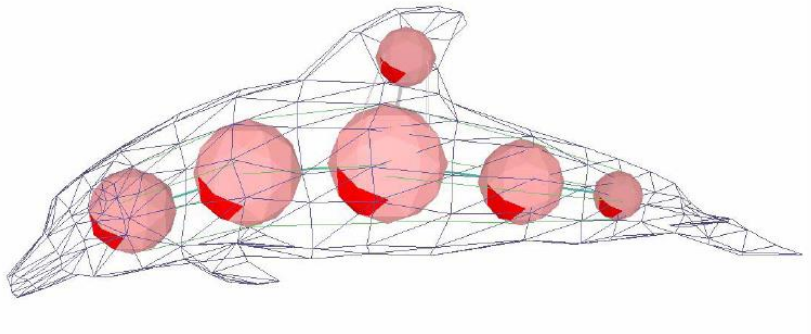
Filling Sphere Approach (3D)



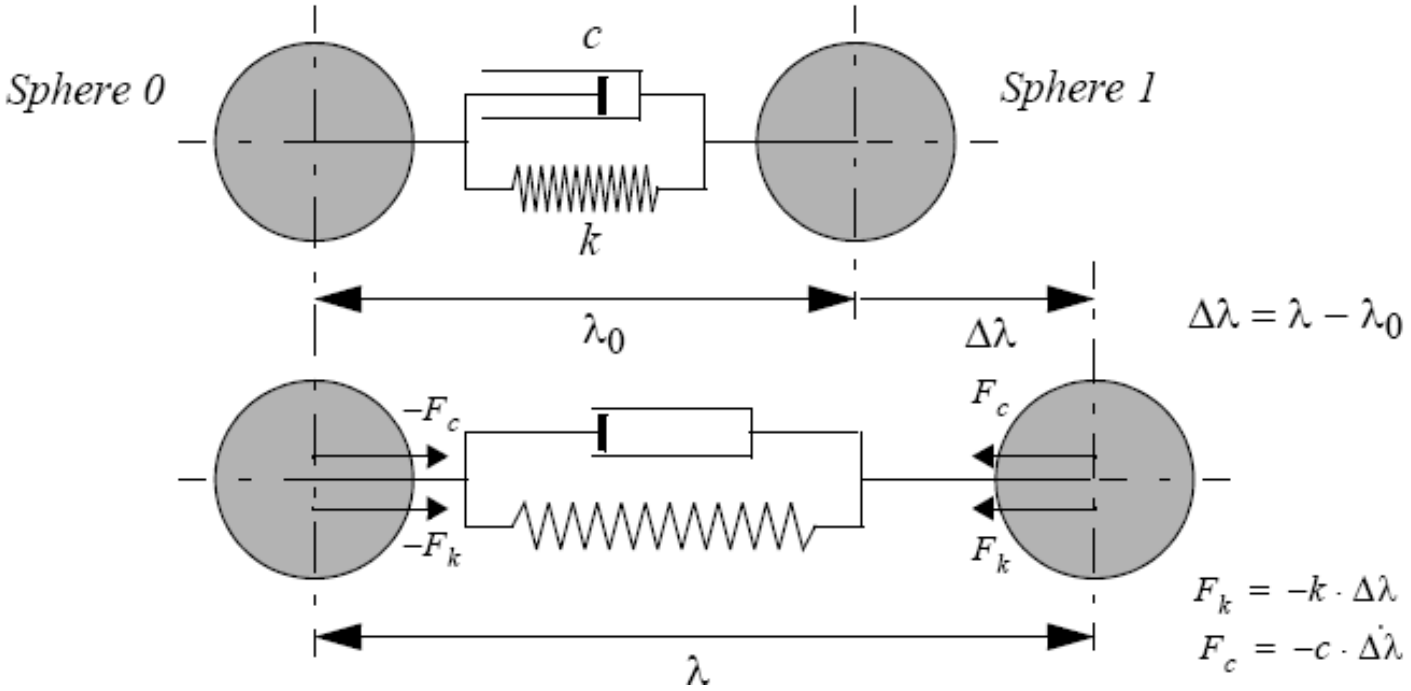
Mass Nodes

Identity	Description	Units	Type
r	*Radius*	$[m]$	Float
ρ	*Density*	$[Kg/m^3]$	Float
m	*Mass*	$[Kg]$	Float
I	*Inertia*	$[Kg \cdot m^2]$	Float $I = \frac{2}{5}mr^2$
$\vec{p}$	*Position of center*	$[m]$	Vector3R $\begin{bmatrix} p_x \\ p_y \\ p_z \end{bmatrix}$
R	*Rotation matrix*	*none*	Matrix33R $\begin{bmatrix} R_{11} & R_{12} & R_{13} \\ R_{21} & R_{22} & R_{23} \\ R_{31} & R_{32} & R_{33} \end{bmatrix}$
$\vec{v}$	*Instantaneous velocity*	$[m/s]$	Vector3R $\begin{bmatrix} v_x \\ v_y \\ v_z \end{bmatrix}$
$\vec{a}$	*Instantaneous acceleration*	$[m/s^2]$	Vector3R $\begin{bmatrix} a_x \\ a_y \\ a_z \end{bmatrix}$
$\vec{F}$	*Force applied on center*	$[N]$	Vector3R $\begin{bmatrix} F_x \\ F_y \\ F_z \end{bmatrix}$
$\vec{M}$	*Moment*	$[N \cdot m]$	Vector3R $\begin{bmatrix} M_x \\ M_y \\ M_z \end{bmatrix}$
$\vec{\omega}$	*Angular velocity*	$[rad/s]$	Vector3R $\begin{bmatrix} \omega_x \\ \omega_y \\ \omega_z \end{bmatrix}$
$\vec{\alpha}$	*Angular acceleration*	$[rad/s^2]$	Vector3R $\begin{bmatrix} \alpha_x \\ \alpha_y \\ \alpha_z \end{bmatrix}$

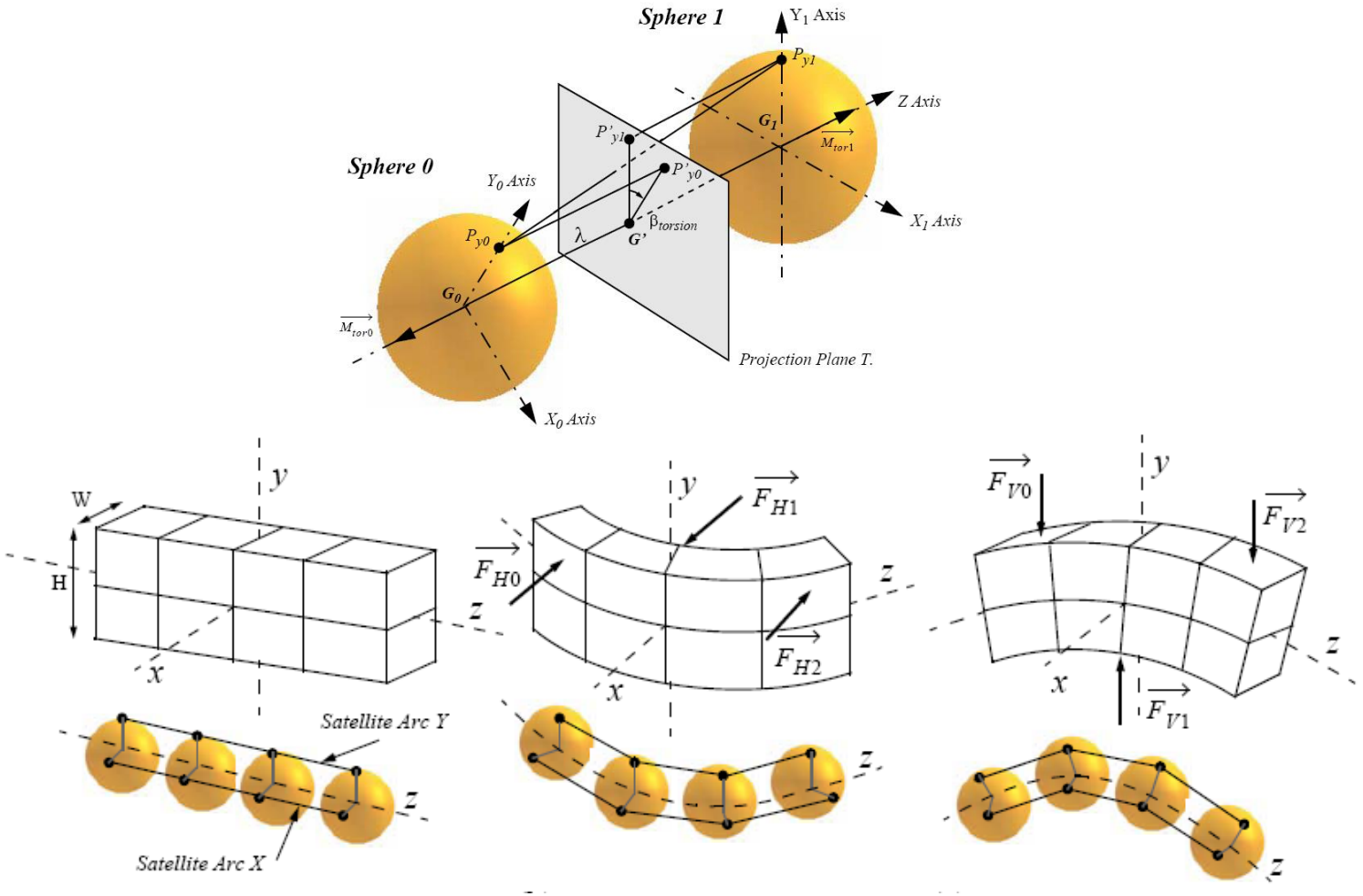




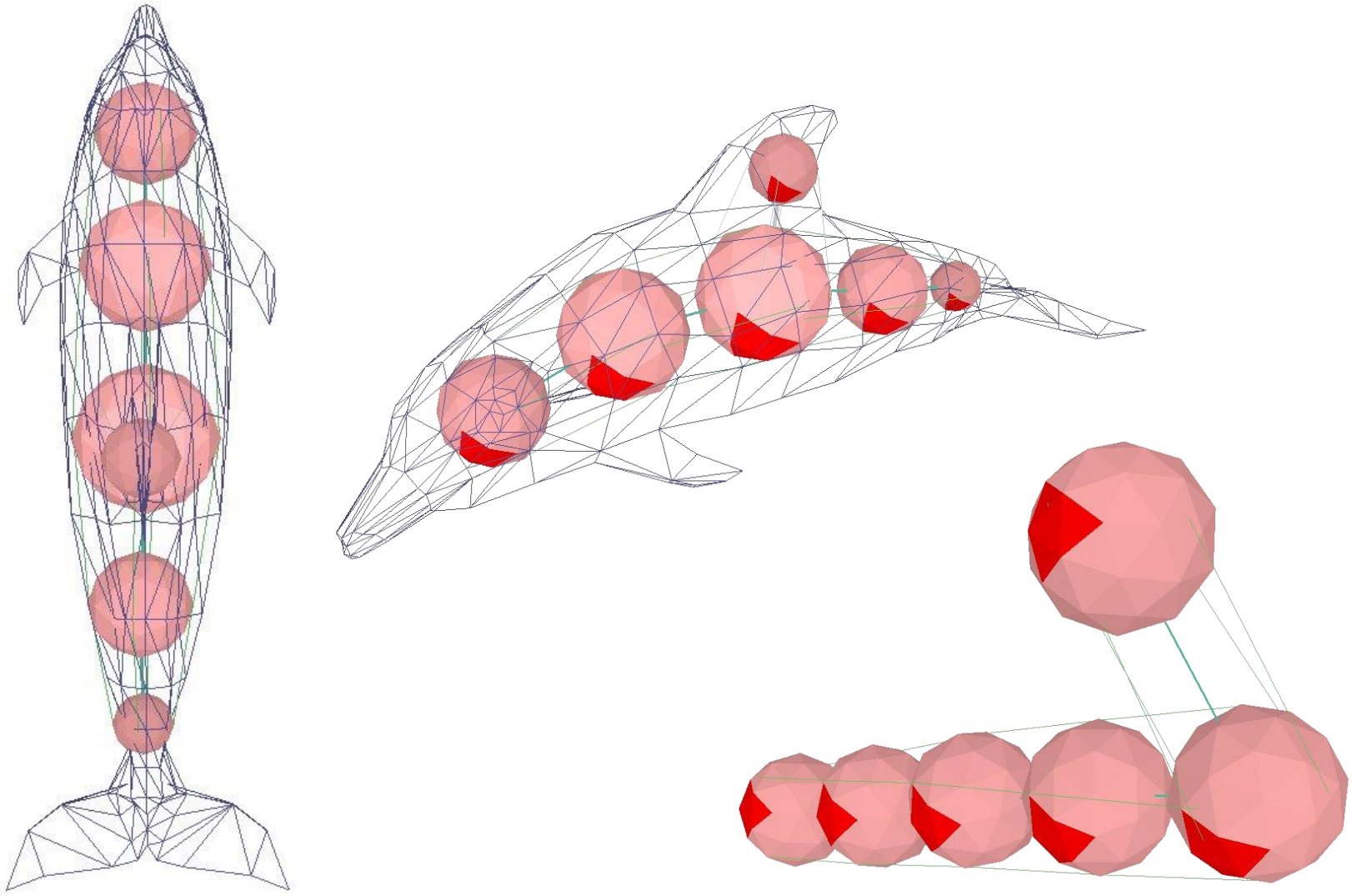
Elongation


Sphere 0
c
Sphere 1
k
λ_0
$\Delta\lambda$
$\Delta\lambda = \lambda - \lambda_0$
$-F_c$
F_c
$-F_k$
F_k
$F_k = -k \cdot \Delta\lambda$
$F_c = -c \cdot \dot{\Delta\lambda}$
λ

Flexion and Torsion



Mesh and Skeleton



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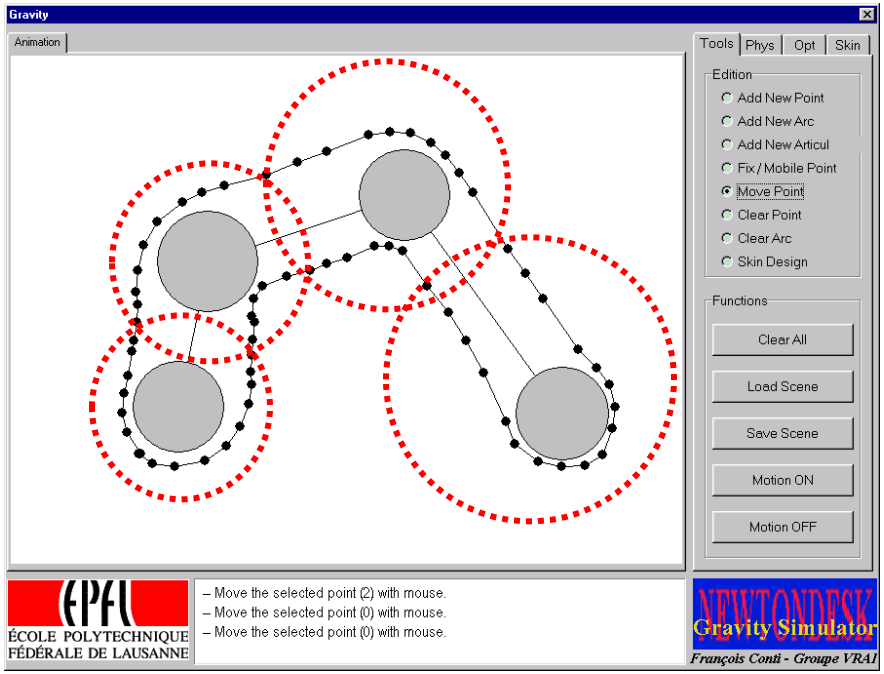
Collision Detection

Collision detection with deformable meshes are difficult to achieve in real time due to the constant change of their geometry (constant update of the collision detection model)

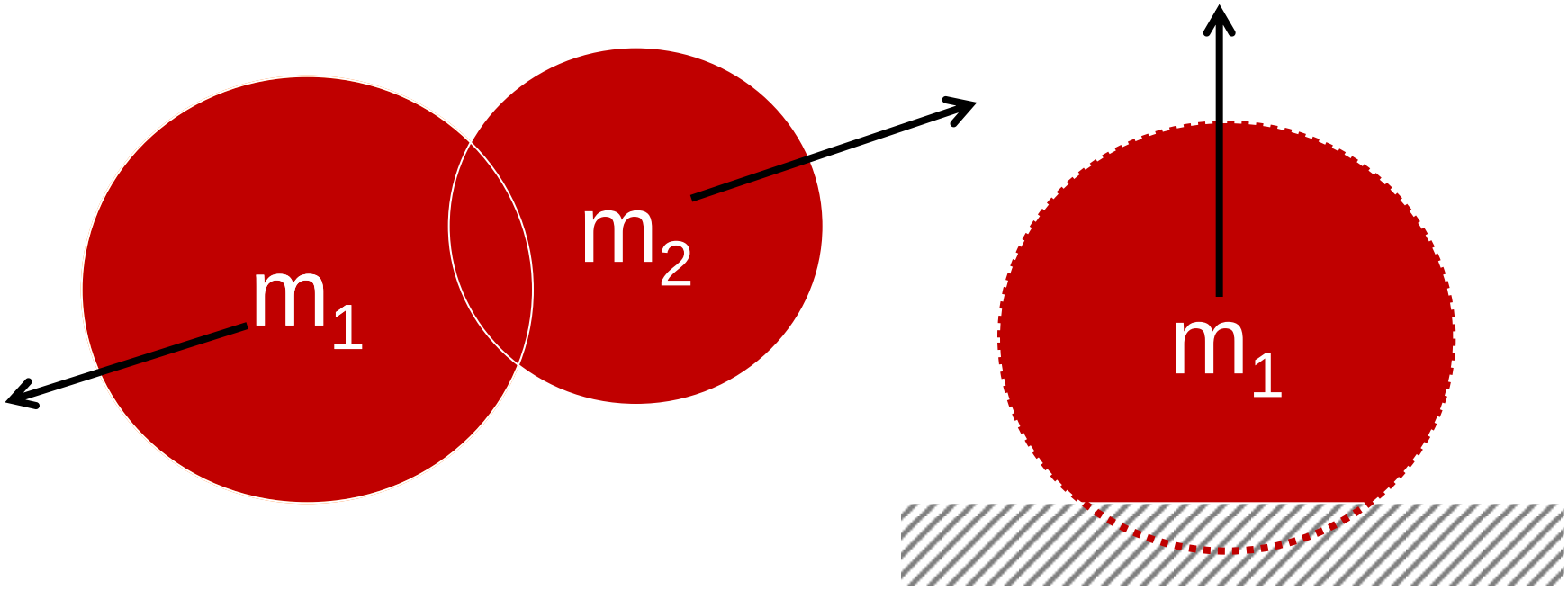
- How can we compute a collision between a segment and deformable mesh?
- How can we compute collisions between deformable meshes?

Collision Segment-Mesh

1. Collision detection is first performed between the input segment and the collision spheres composing the skeleton of the model.
2. Collision between the segment and the triangles are then searched locally



Collision Mesh-Mesh



Reaction forces are computed between mass nodes

$F_r = - k\, x$

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